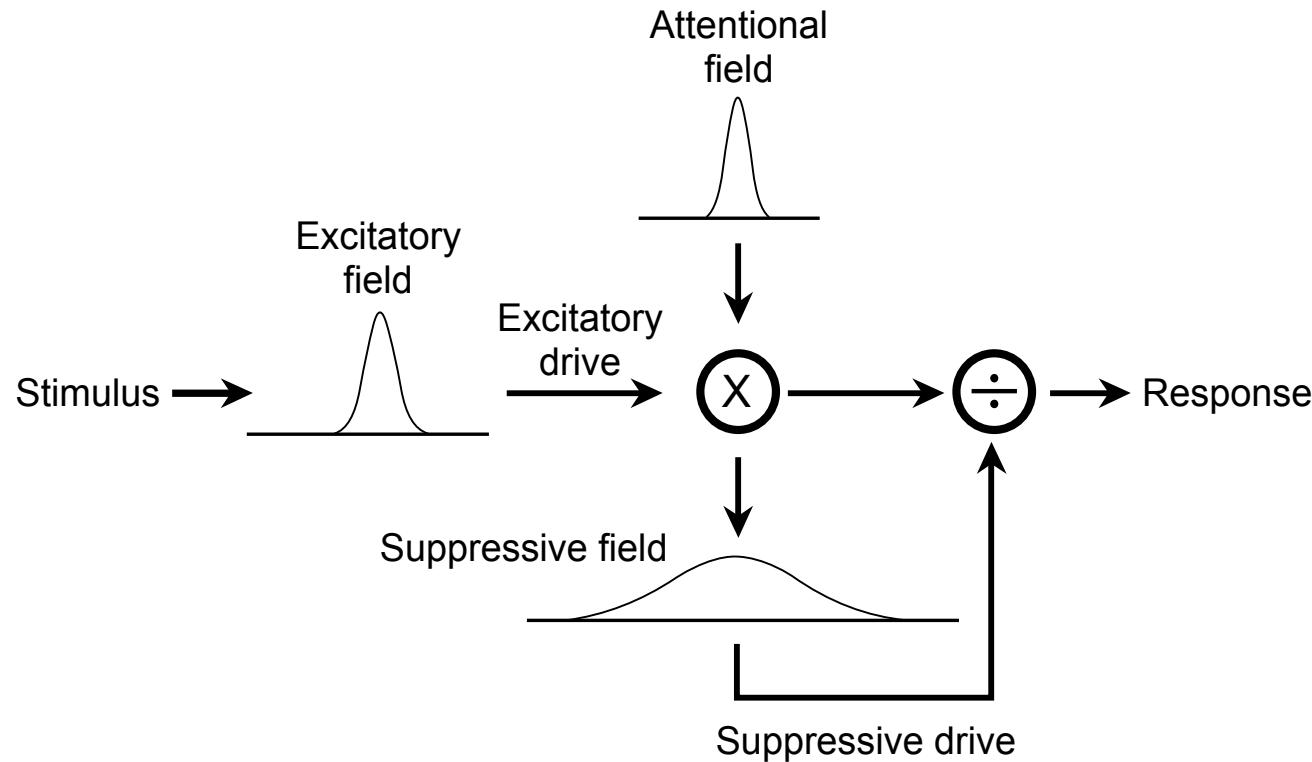


# The Normalization Model of Attention

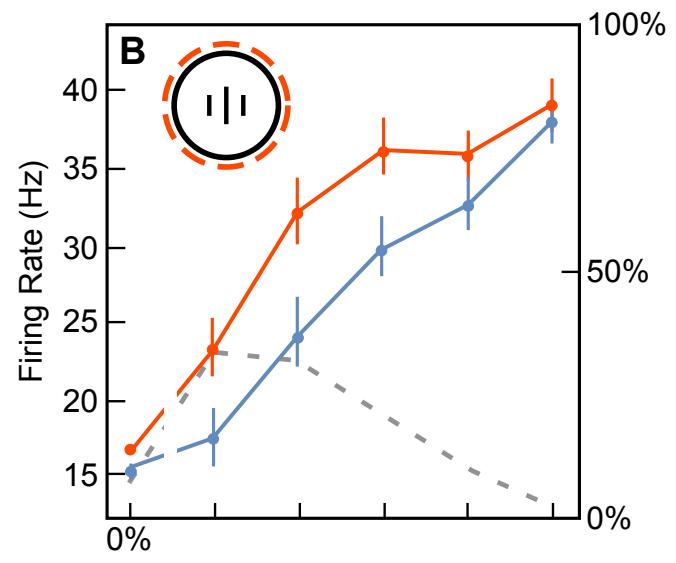
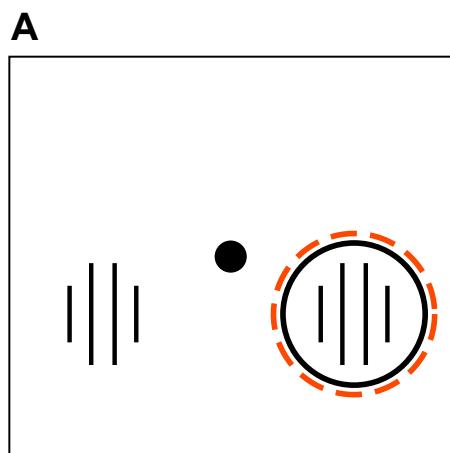


David J. Heeger  
NYU

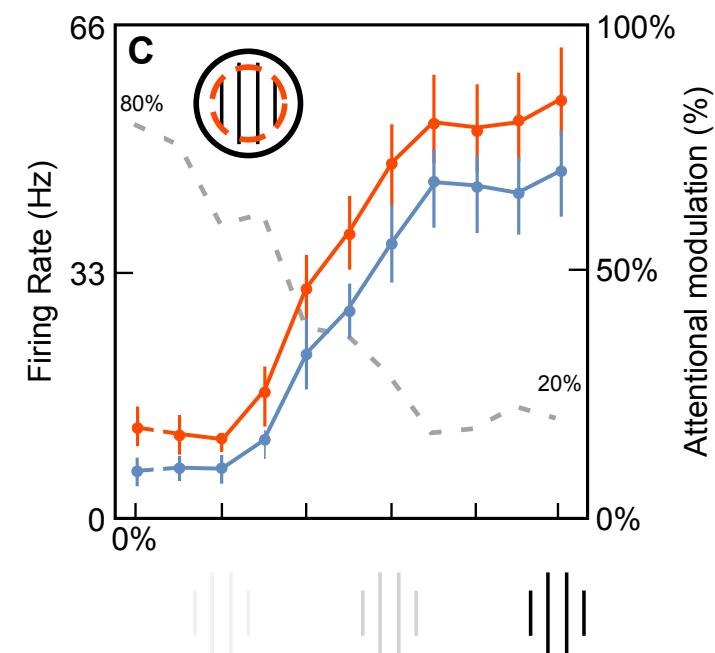
John H. Reynolds  
Salk

# Contrast gain & response gain

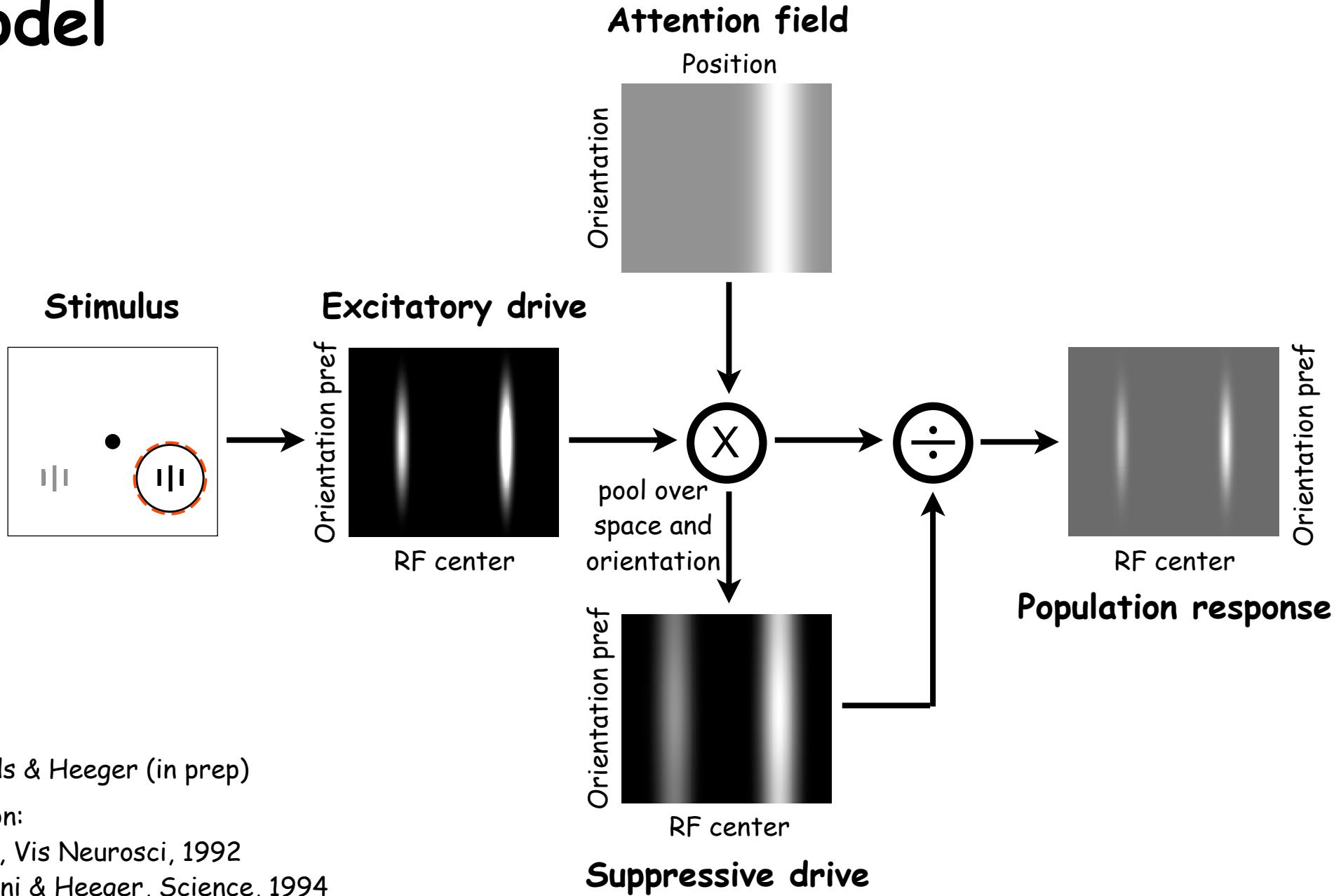
Reynolds, Pasternak, &  
Desimone, Neuron, 2000



Williford & Maunsell,  
J Neurophysiol, 2006



# Model



Reynolds & Heeger (in prep)

Based on:

Heeger, Vis Neurosci, 1992

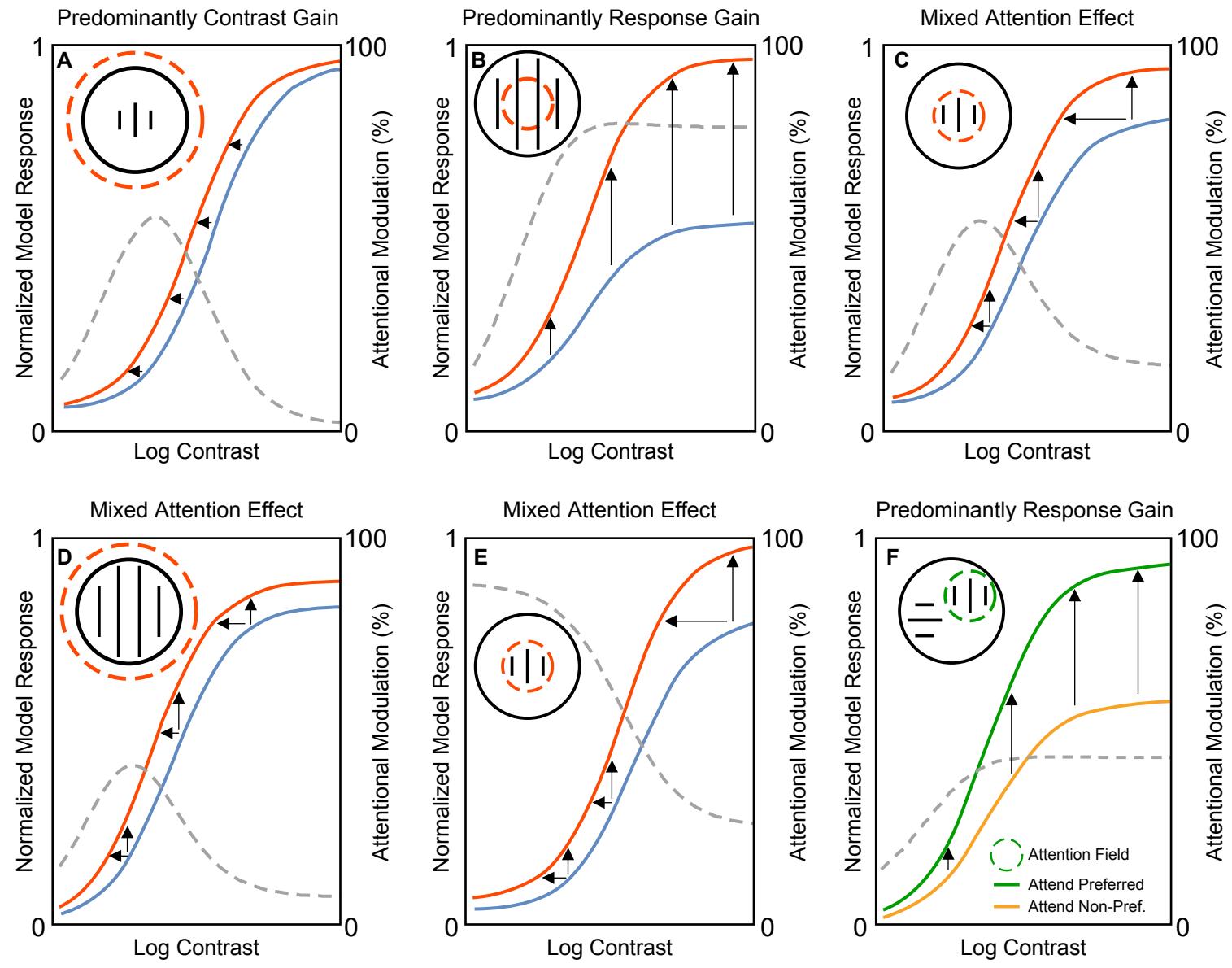
Carandini & Heeger, Science, 1994

Carandini, Heeger & Movshon, J Neurophysiol, 1997

Cavanaugh, Bair, & Movshon, J Neurophysiol, 2002

Reynolds & Chelazzi, Ann Rev Neurosci, 2004

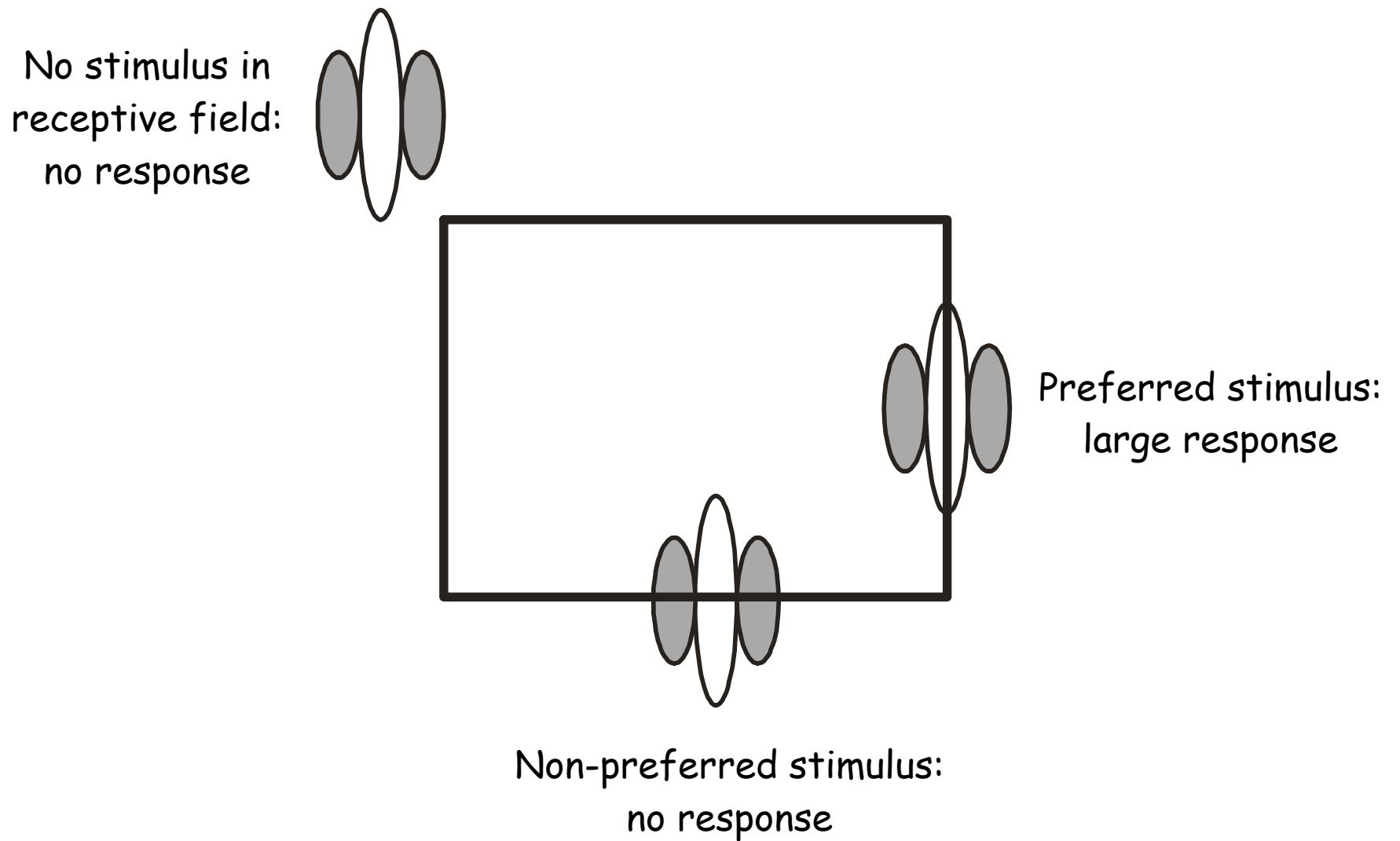
# Simulated responses



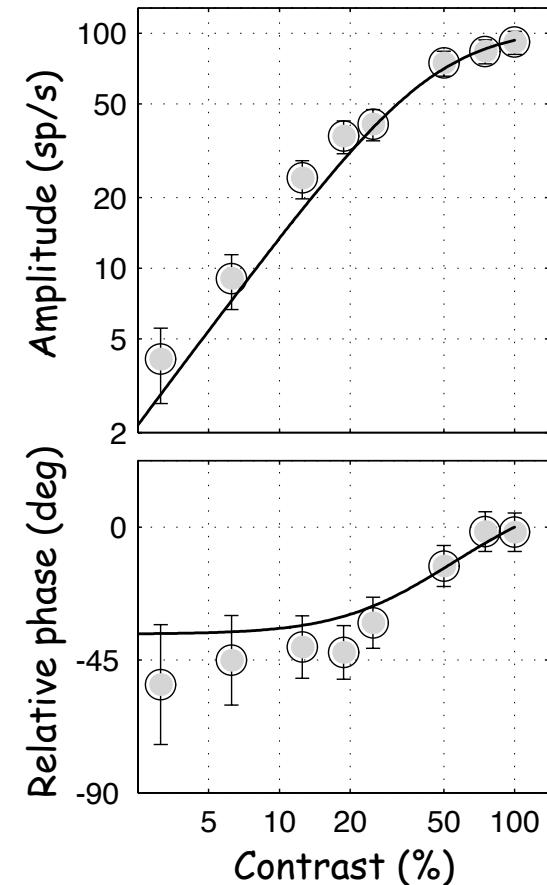
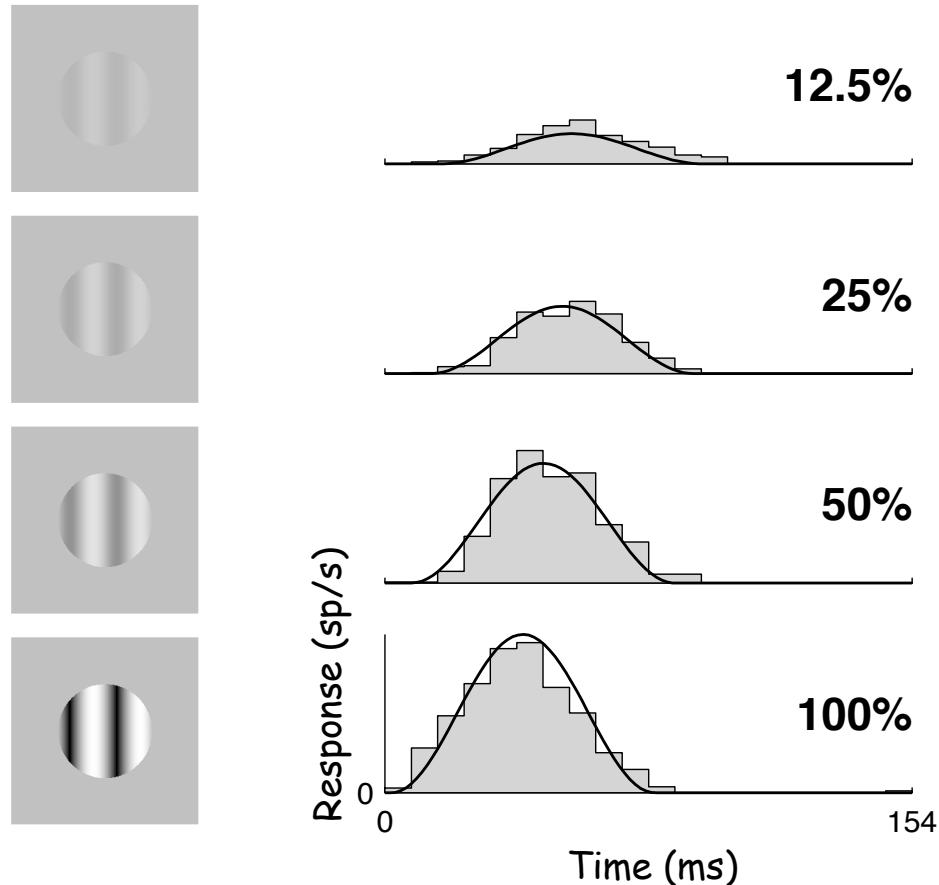
Legend:

- Receptive Field (Black circle)
- Attention Field (Orange dashed circle)
- Stimulus (Vertical bars)
- Ignored (Blue line)
- Attended (Red line)
- % Attentional Modulation (Dashed grey line)
- Attention Field (Green dashed circle)
- Attend Preferred (Green line)
- Attend Non-Pref. (Orange line)

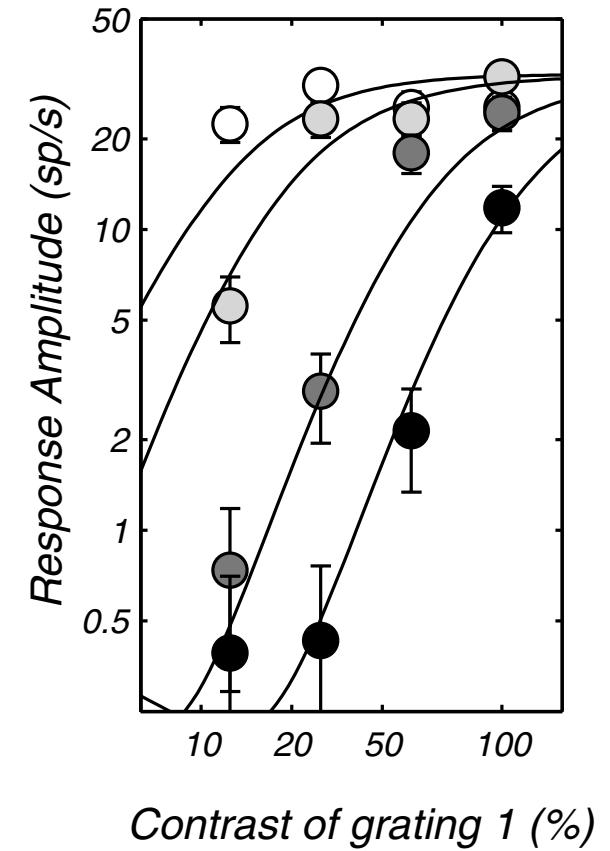
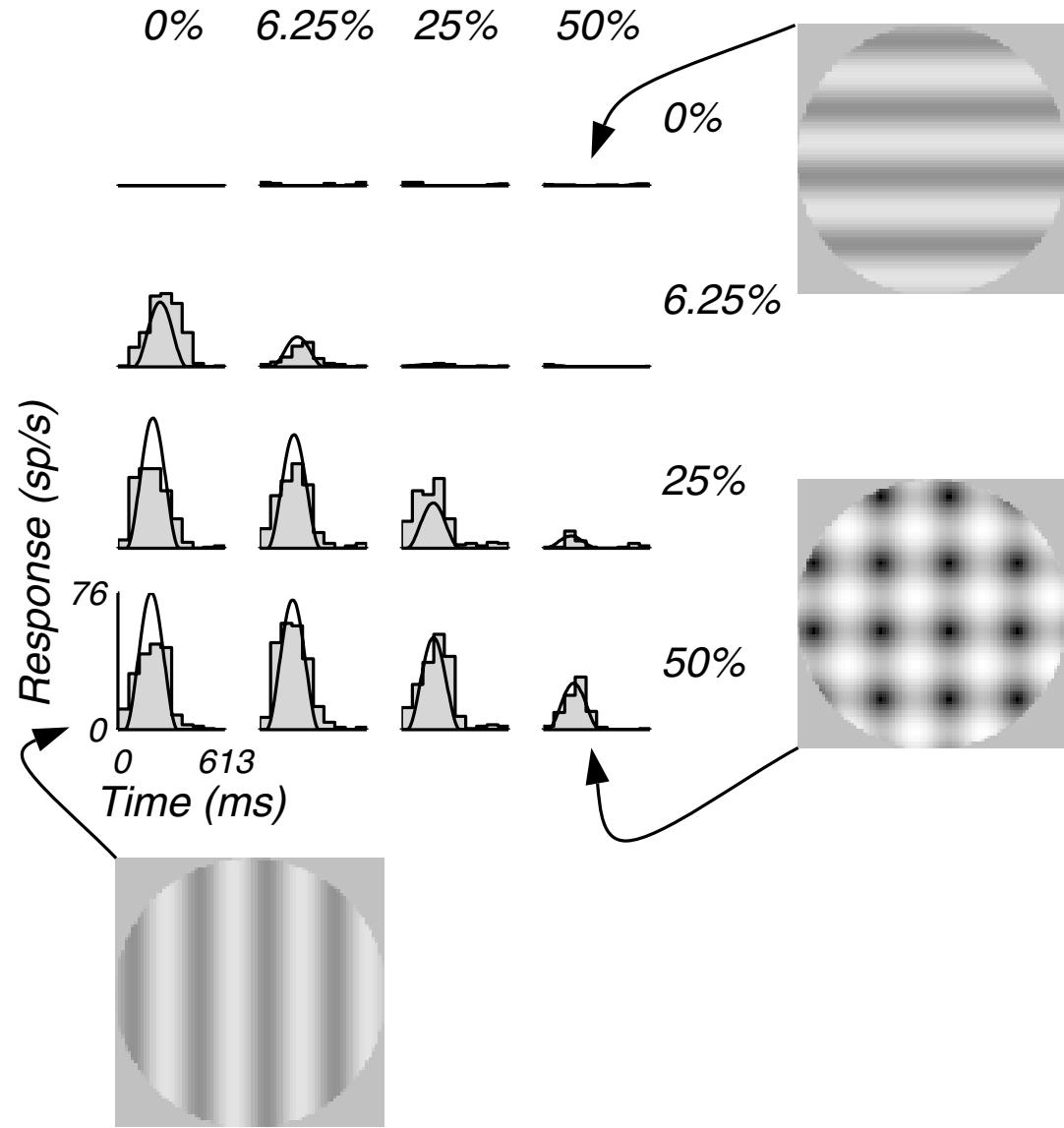
# Orientation selectivity model



# Response saturation and phase advance

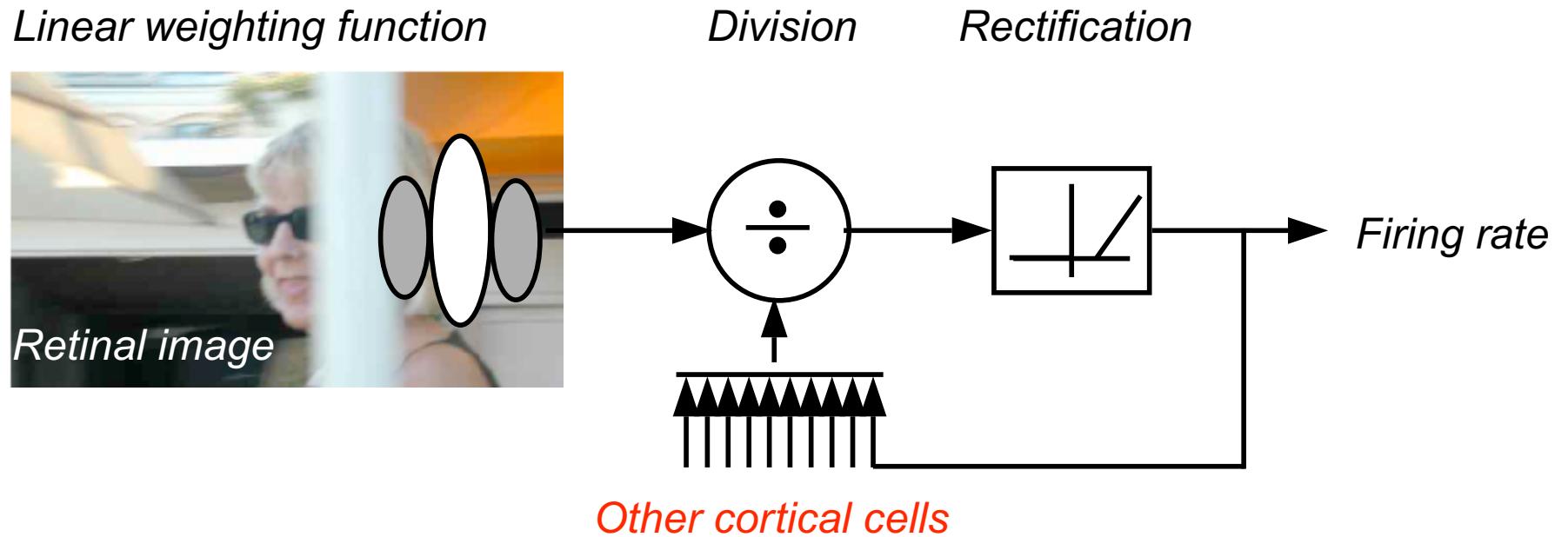


# Masking



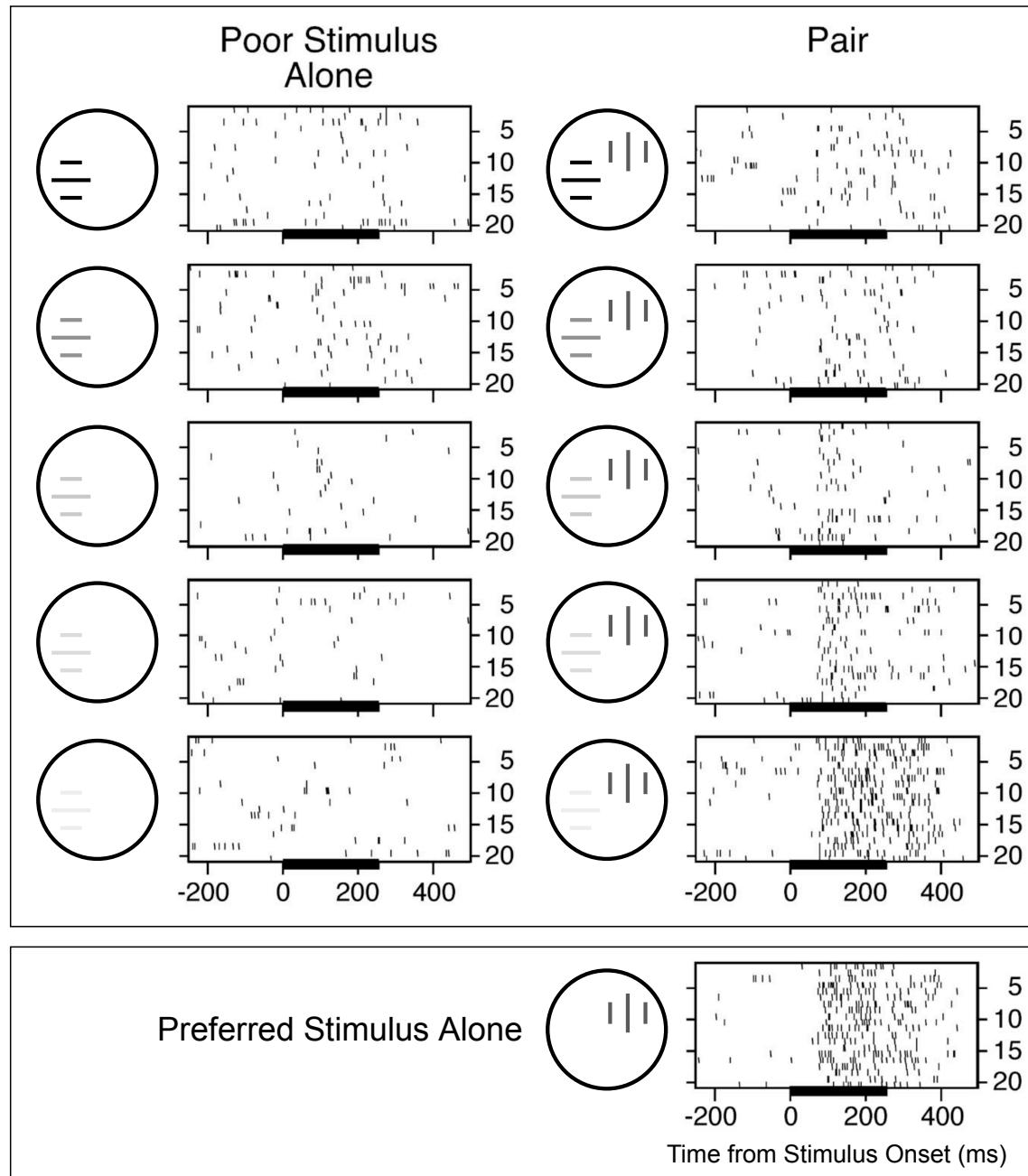
Carandini, Heeger & Movshon, J Neurosci, 1997

# Normalization model



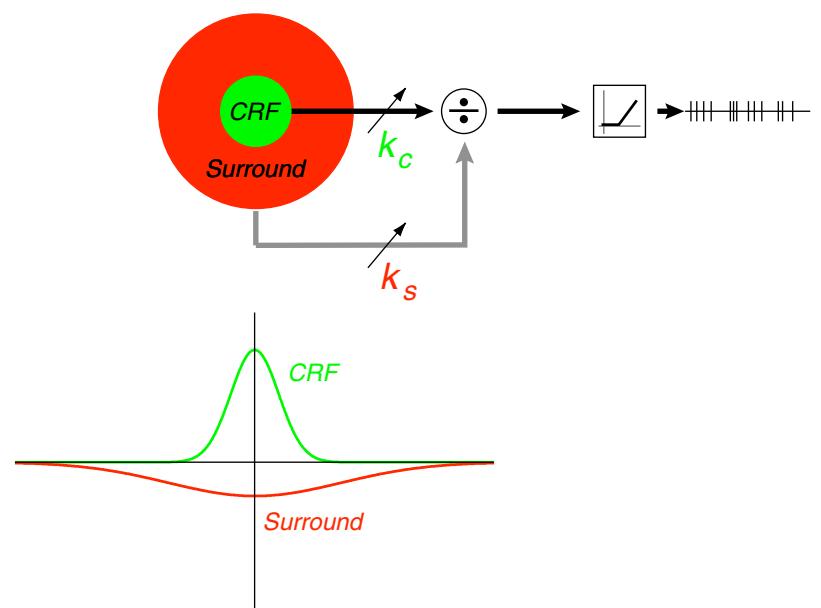
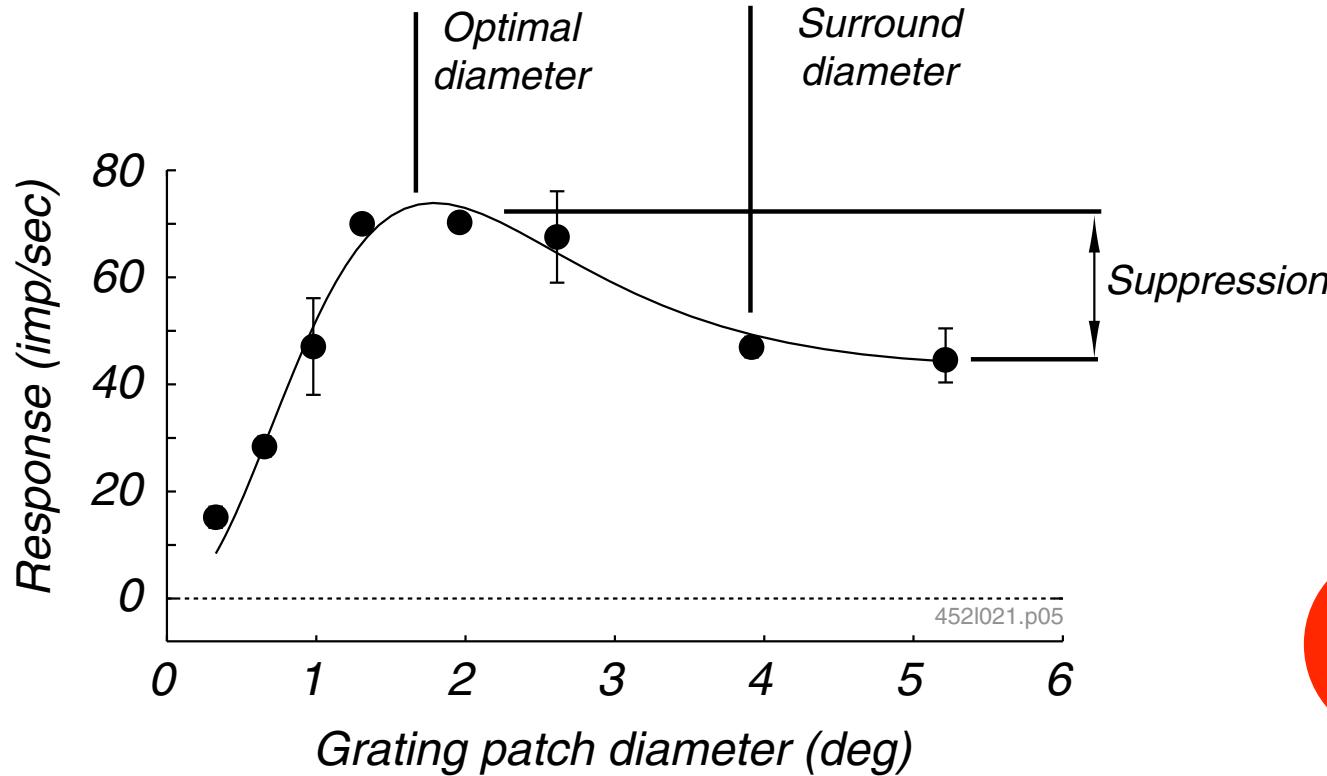
$$\text{normalized response} = \frac{\text{unnormalized response}}{\sum \text{unnormalized responses} + \sigma}$$

# Normalization in V4

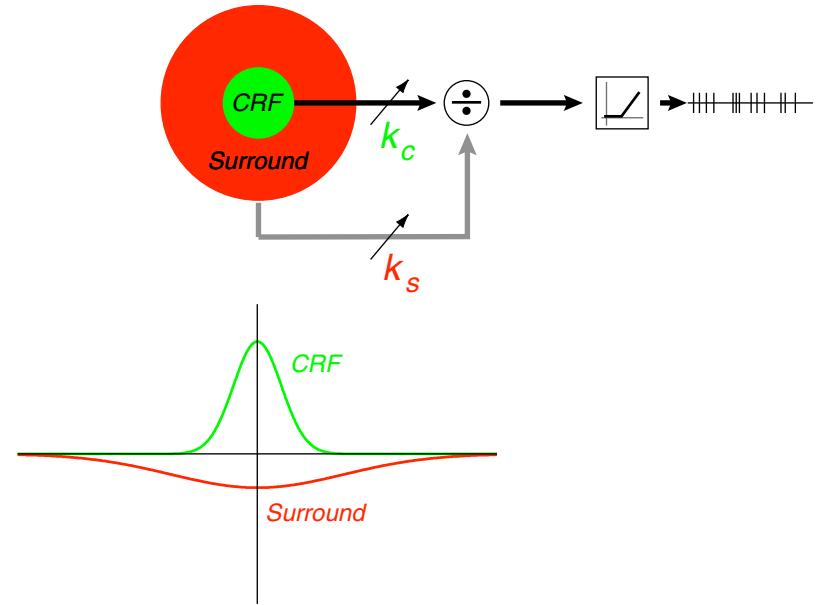
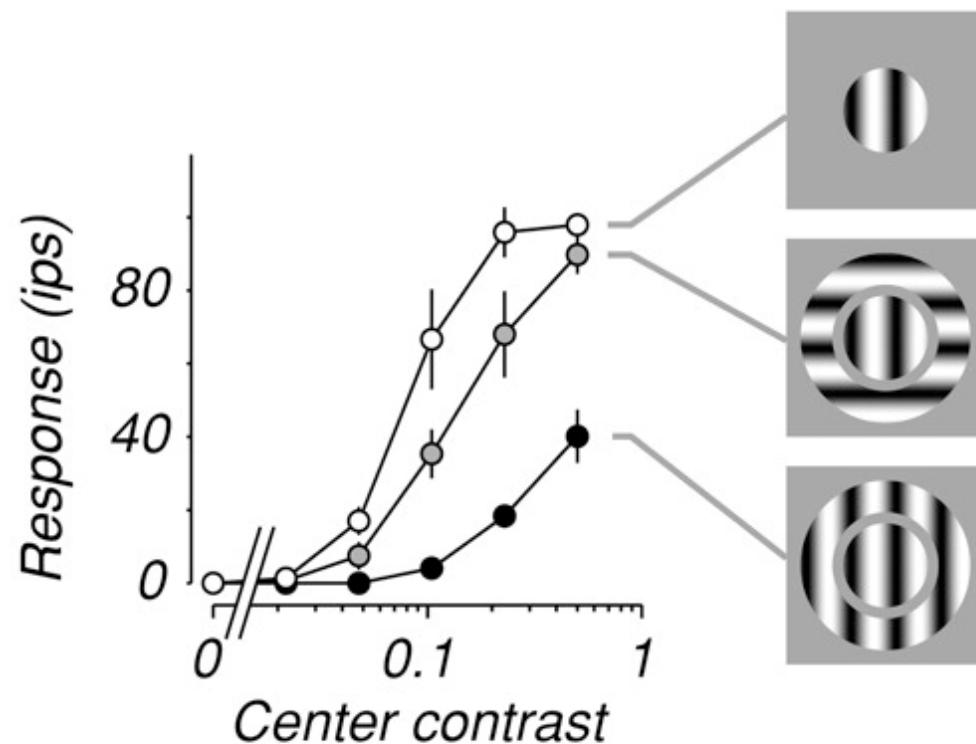


Reynolds &  
Desimone,  
Neuron, 2003

# Surround suppression & normalization



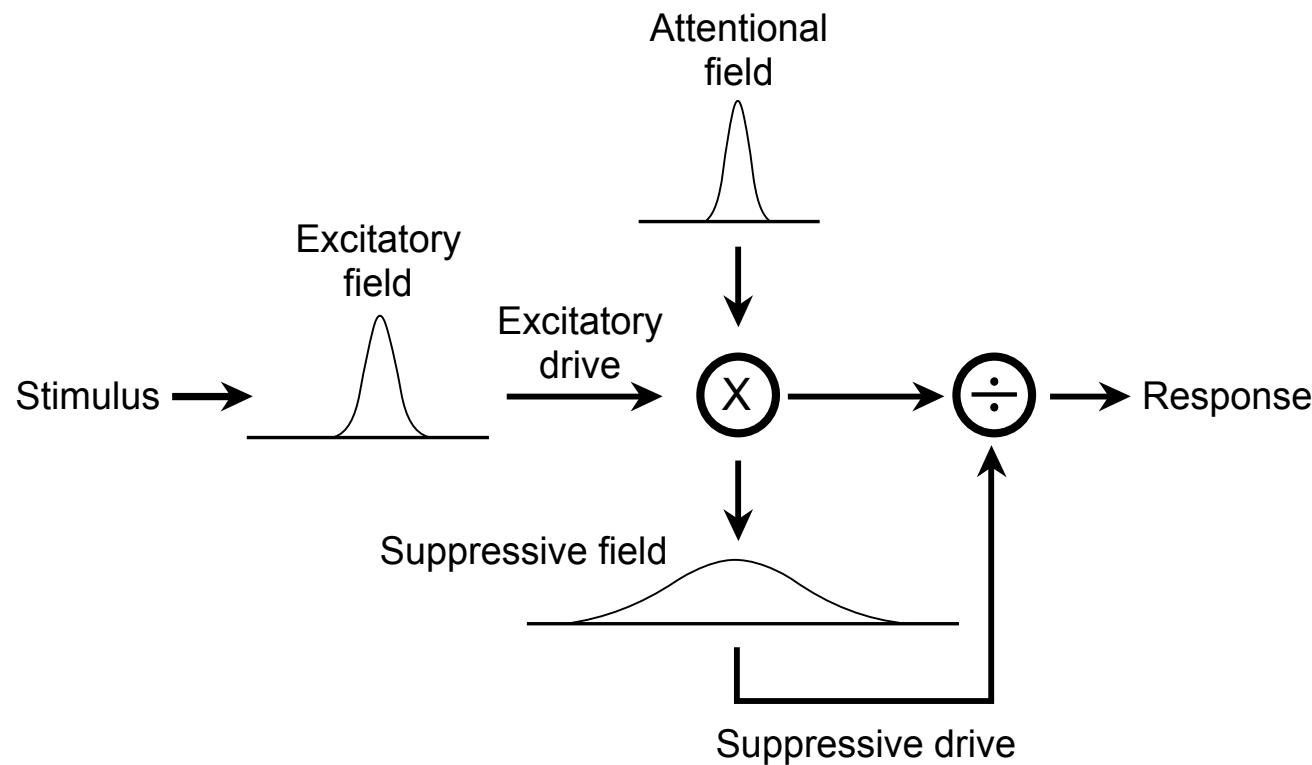
# Surround suppression & normalization



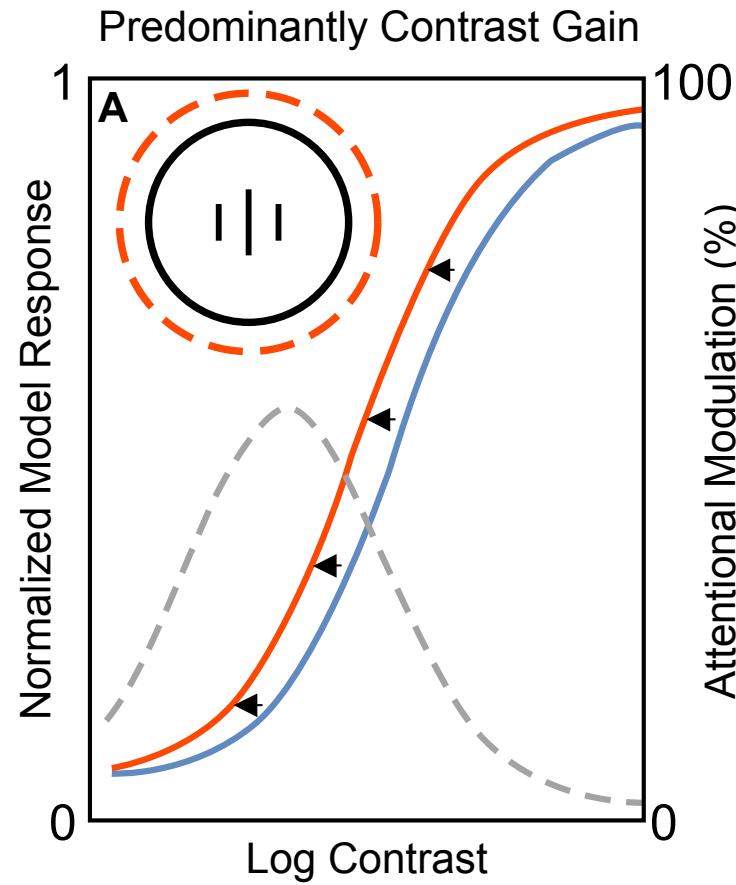
$$R = \alpha \frac{c}{c + \beta c_s + \sigma}$$

$0 < \beta < 1$  surround suppression

# Normalization model of attention



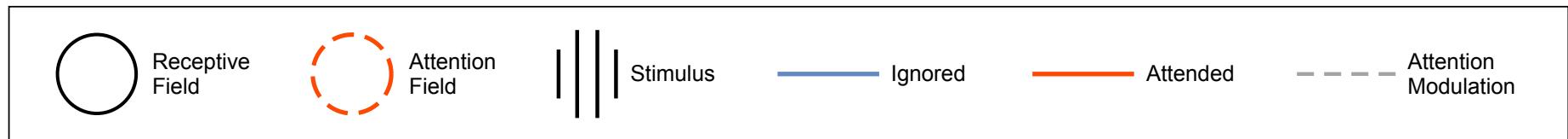
# Small stimulus, large attention field



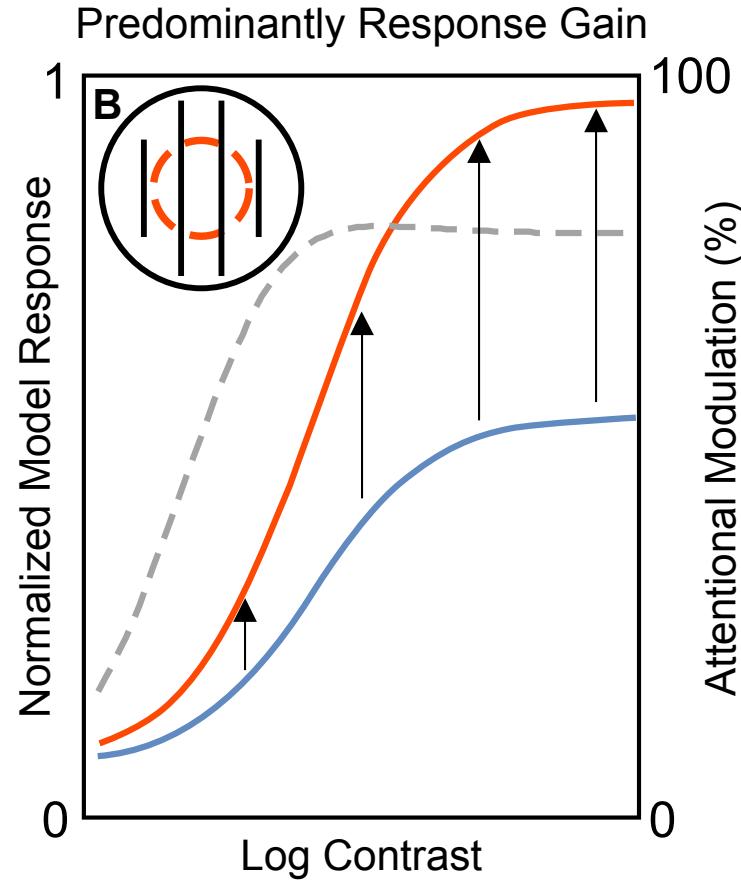
$$R = \alpha \frac{c}{c + \sigma}$$

$$R = \alpha \frac{\gamma c}{\gamma c + \sigma} = \alpha \frac{c}{c + \sigma / \gamma}$$

$\gamma > 1$  attentional gain affects excitatory drive and suppressive drive equally



# Large stimulus, small attention field



$$R = \alpha \frac{c}{c + \beta c + \sigma}$$

For  $c \gg \sigma$      $R = \alpha \frac{1}{1 + \beta}$

$$R = \alpha \frac{\gamma c}{\gamma c + \beta c + \sigma}$$

For  $c \gg \sigma$      $R = \alpha \frac{\gamma}{\gamma + \beta}$

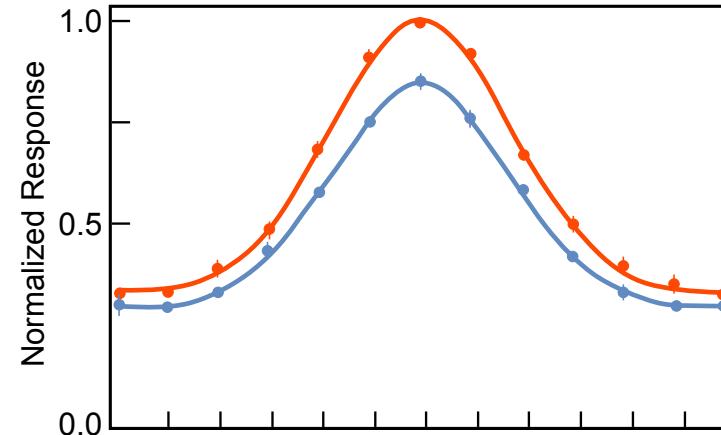
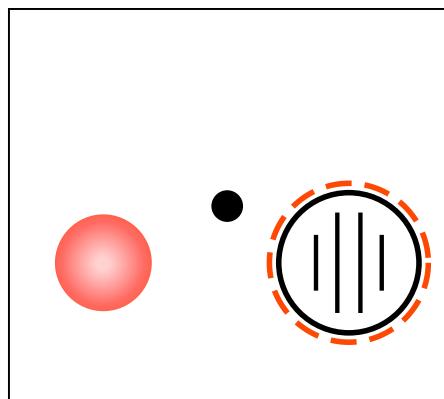
$\gamma > 1$  attentional gain

$0 < \beta < 1$  surround suppression

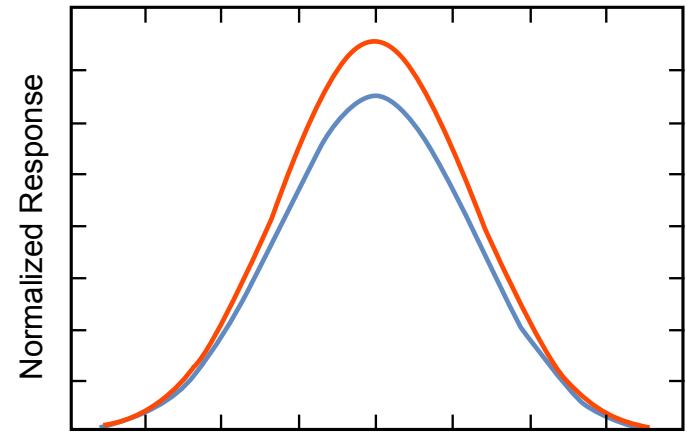


# Spatial attention scales tuning curve

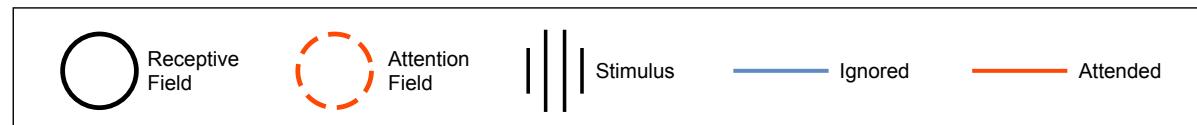
McAdams & Maunsell,  
J Neurosci, 1999



Model



One stimulus within  
receptive field and the  
other contralateral.

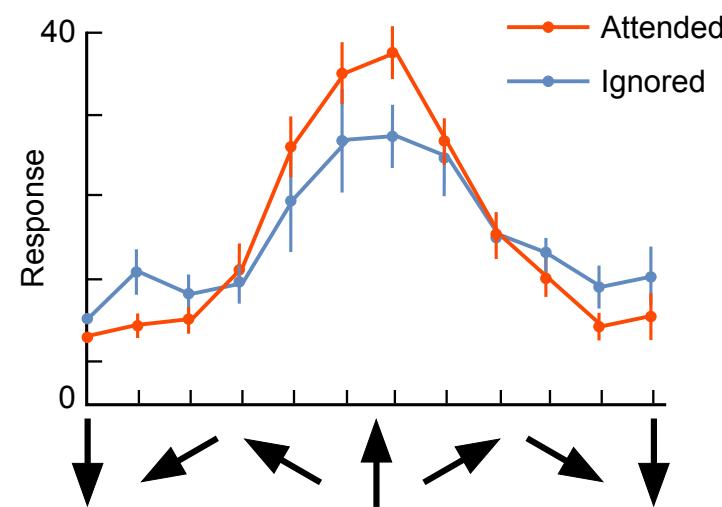
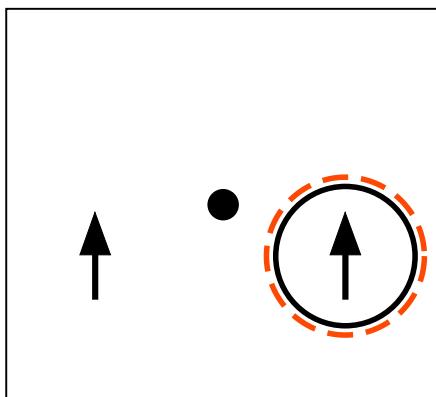


$$R(c, \theta) = \alpha R(c) R(\theta)$$

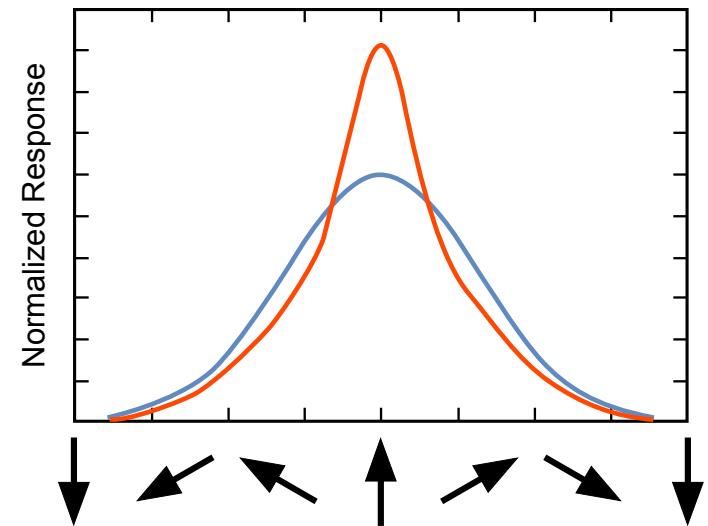
Separable function of contrast and orientation; change in response gain or contrast gain affects only  $R(c)$ .

# Featural attention can sharpen tuning curves

Treue & Martinez-Trujillo,  
Nature, 1999



Model



Two stimuli moved same direction on each trial, one within receptive field, and other in opposite hemifield. Attend fixation or attend same motion in opposite hemifield.

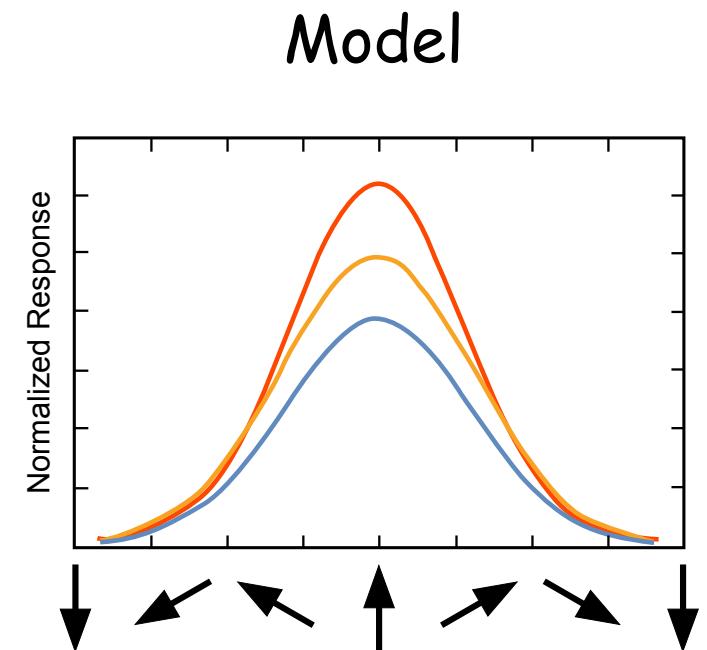
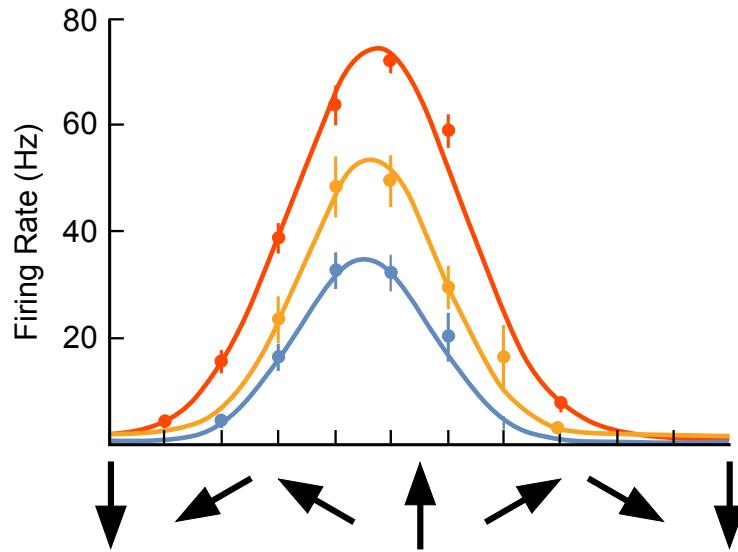
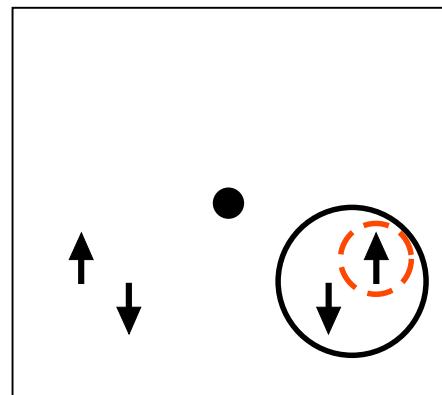
$$R(\theta) = \alpha A(\theta) E(\theta)$$

Attention field

Excitatory drive

# Attention can increase or decrease gain (selection)

Martinez-Trujillo & Treue,  
Curr Biol, 2004



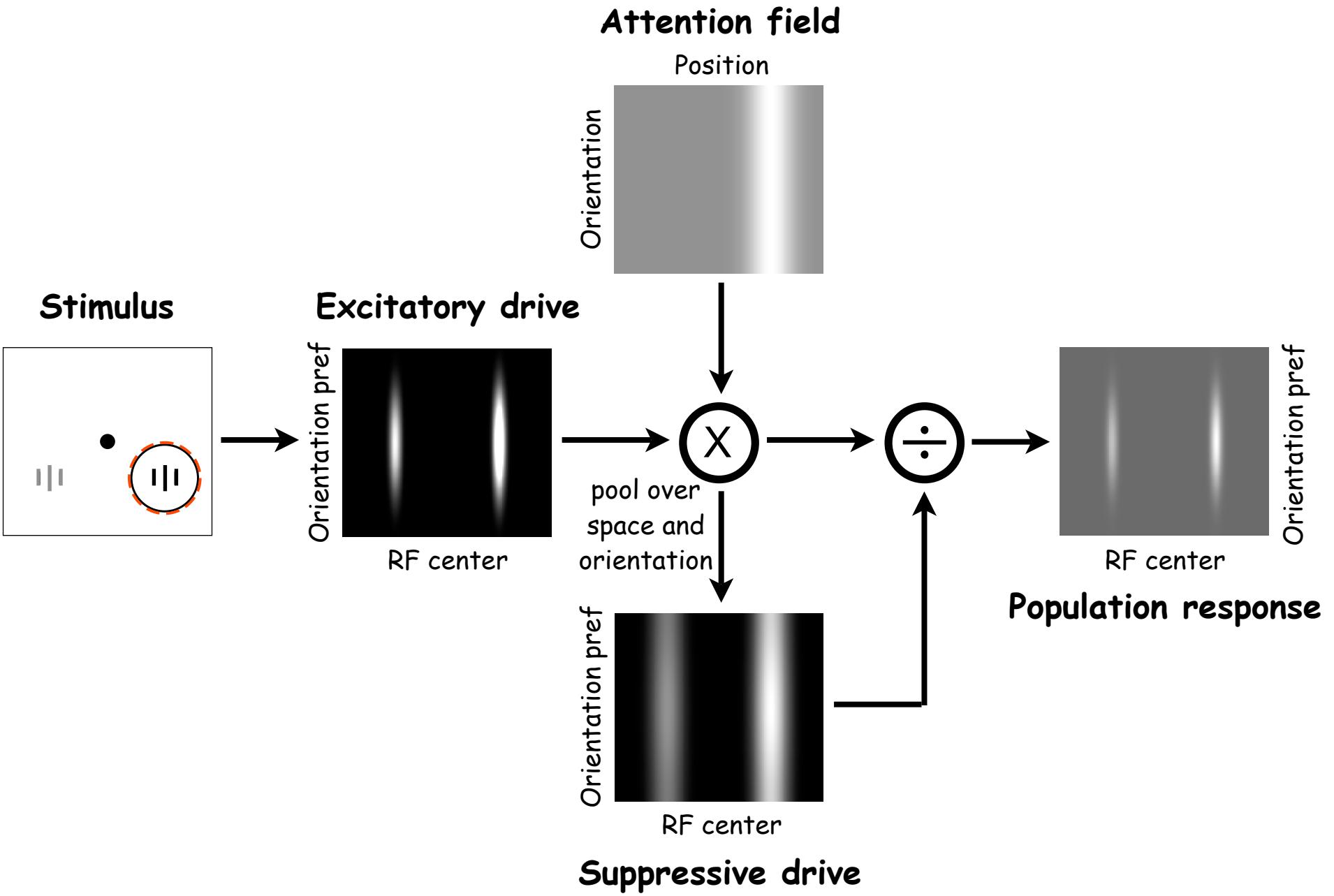
Two stimuli within receptive field.  
One moved in non-preferred  
direction. Other direction varied.

$$R_f(\theta) = \alpha E(\theta) / (k + \sigma)$$

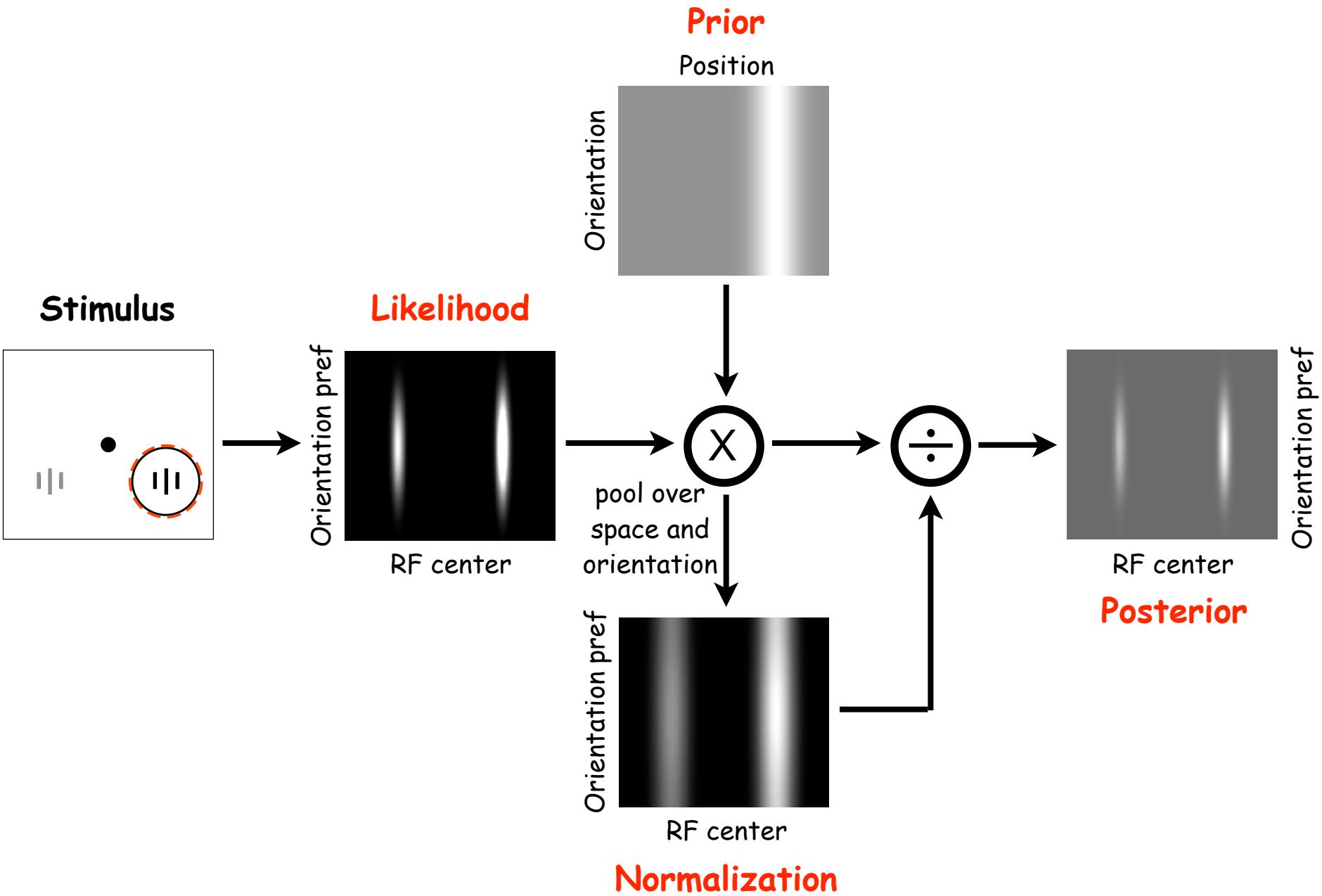
$$R_n(\theta) = \alpha E(\theta) / (\gamma k + \sigma)$$

$$R_v(\theta) = \alpha A(\theta) E(\theta) / (\gamma k + \sigma)$$

# Bayesian inference



# Bayesian inference



# Hierarchical Bayesian Inference

